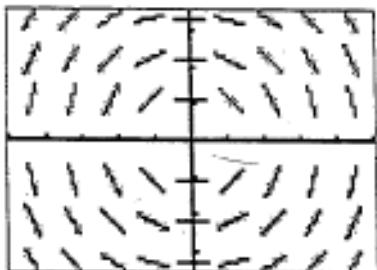


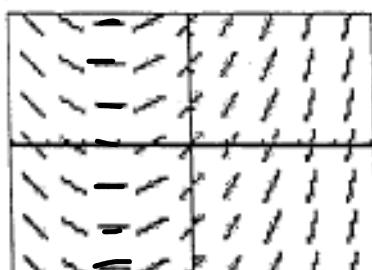
## Opener

Match the slope fields with their differential equations.

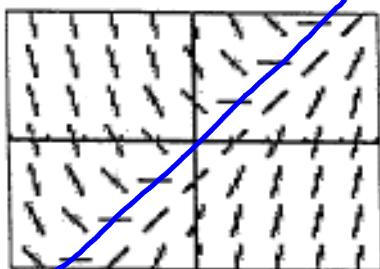
(A)



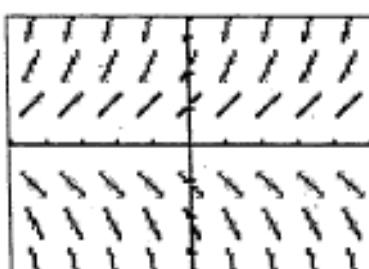
(B)



(C)



(D)



$$15. \frac{dy}{dx} = \frac{1}{2}x + 1 \quad \text{B}$$

$$\frac{1}{2}x + 1 = 0$$

$$\frac{1}{2}x = -1$$

$$16. \frac{dy}{dx} = y \quad \text{D}$$

$$x = -2$$

$$17. \frac{dy}{dx} = x - y \quad \text{C}$$

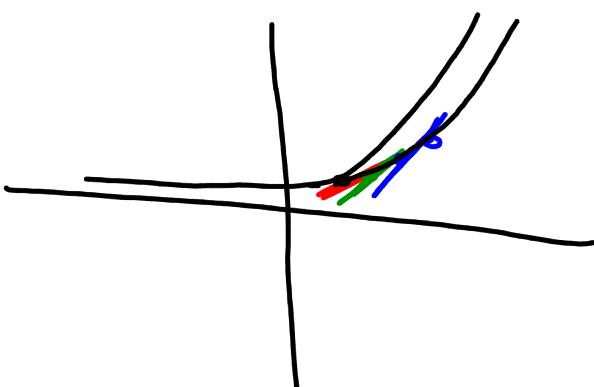
$$18. \frac{dy}{dx} = -\frac{x}{y} \quad \text{A}$$

## 6-1 day 3 Euler's Method

### Learning Objectives:

I can use Euler's Method to estimate the value of a function at a given point

Euler's Method is a way to create the graph of a function given its derivative and a point on the graph. This is meant to be used when you can't find the antiderivative of the function.



$$\frac{dy}{dx} = f(x, y)$$

ic  $(x_1, y_1)$

## Euler's Method

1. Begin w/point  $(x, y)$  specified by the initial condition. This MUST be a point on the graph of  $f(x)$ .
2. Use the differential equation to find the slope of the tangent line at  $(x, y)$
3. Increase  $x$  by some small amount ( $\Delta x$ ).
4. Calculate  $\Delta y$  using the formula 
$$\boxed{\Delta y = \frac{dy}{dx} \cdot \Delta x}$$
5. This defines a new point  $(x + \Delta x, y + \Delta y)$  which is not on the graph of  $f(x)$  but on the tangent line and is "sufficiently close" to  $f(x)$ .
6. Use this new point and repeat steps 1-3.

**NOTE:** To construct the approximation of the graph of  $f(x)$  to the left of  $x$ , use negative values of  $\Delta x$ .

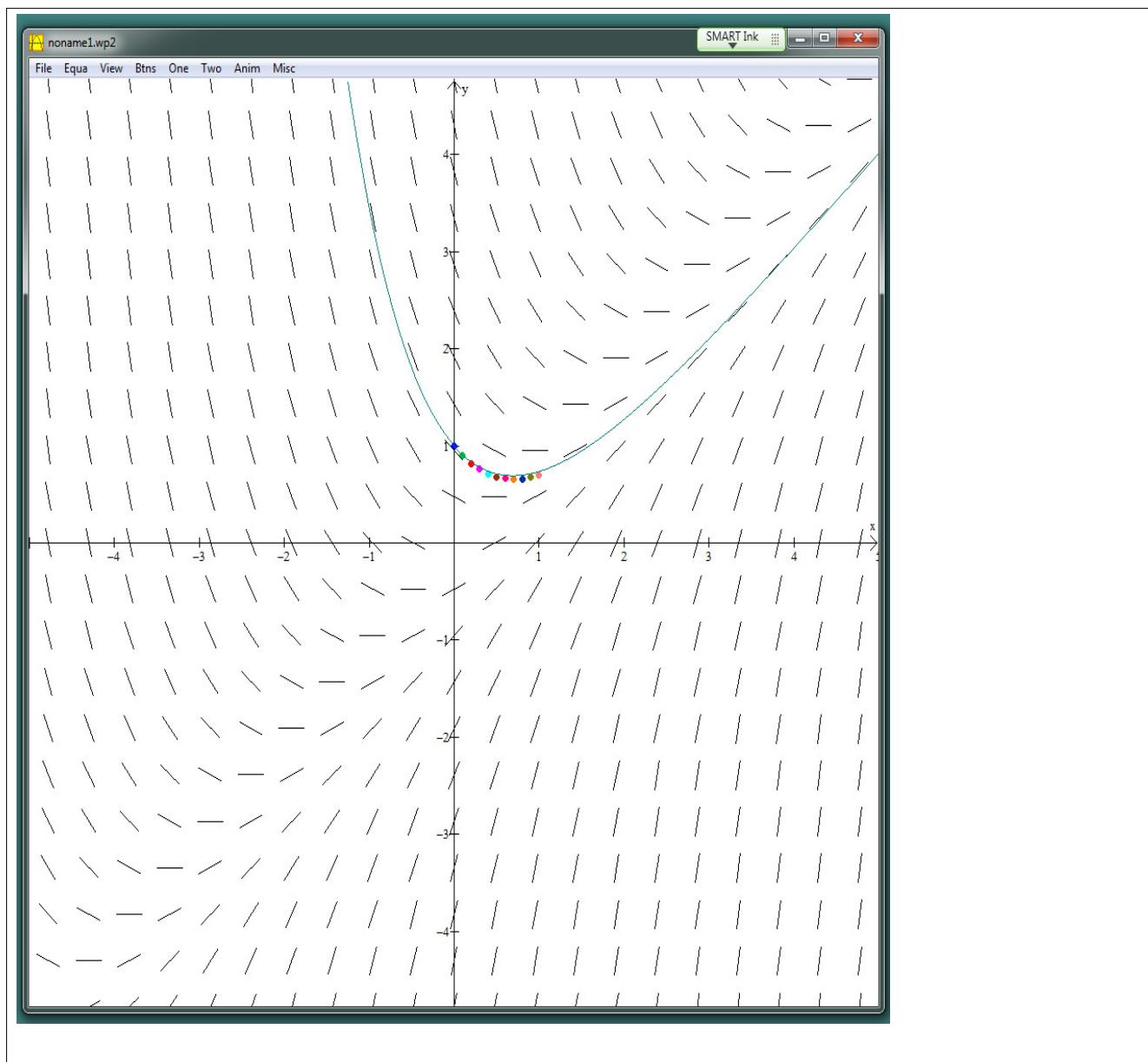
Ex1. Let  $f$  be the function with derivative  $\frac{dy}{dx} = x - y$

with initial condition  $(0,1)$ . Use Euler's Method and increments of  $\Delta x = .1$  to approximate  $f(1)$

Cards Method - To create a graph of a function given its derivative & a point on the graph

$(x, y)$	$\frac{dy}{dx}$	$\Delta x$	$\Delta y = \frac{dy}{dx} \Delta x$	$(x + \Delta x, y + \Delta y)$
(0, 0)	-1	0.1	-0.1	(0.1, 0.1)
(0.1, 0.1)	-0.8	0.1	-0.08	(0.2, 0.82)
(0.2, 0.82)	-0.62	0.1	-0.062	(0.3, 0.758)
(0.3, 0.758)	-0.458	0.1	-0.0458	(0.4, 0.712)
(0.4, 0.712)	-0.3172	0.1	-0.03172	(0.5, 0.68018)
(0.5, 0.68018)	-0.18048	0.1	-0.018048	(0.6, 0.66288)
(0.6, 0.66288)	-0.06728	0.1	-0.006728	(0.7, 0.6566)
(0.7, 0.6566)	0.0474	0.1	0.00474	(0.8, 0.66044)
(0.8, 0.66044)	0.13906	0.1	0.13906	(0.9, 0.67488)
(0.9, 0.67488)	0.27515	0.1	0.07515	(1.0, 0.69737)

$$f(1) \approx .697$$



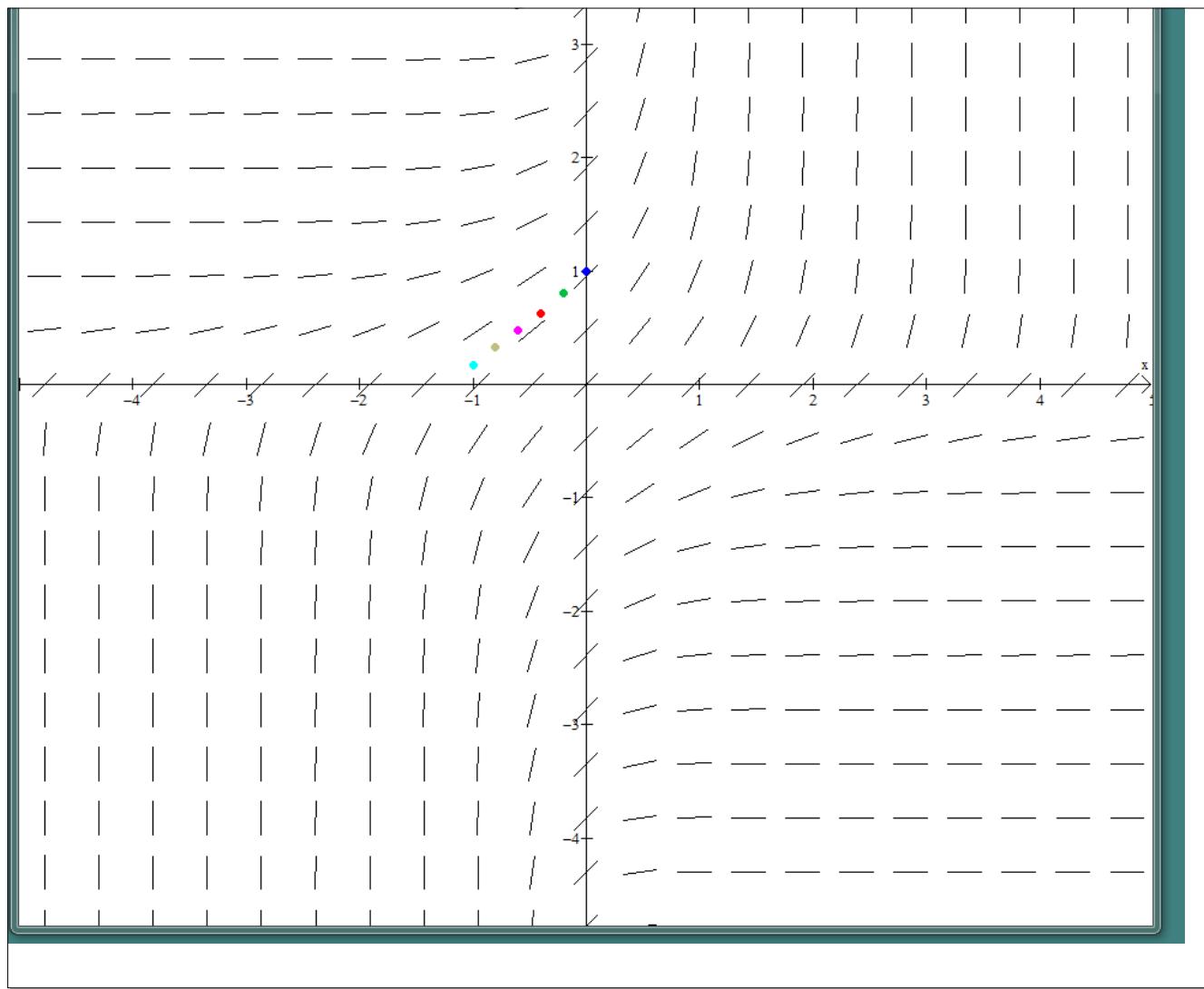
Ex2. Given the differential equation  $\frac{dy}{dx} = e^{xy}$  with initial condition (0,1). Use Euler's Method and increments of  $\Delta x = .2$  to approximate f(-1)

$(x, y)$	$\frac{dy}{dx}$	$\Delta x$	$\Delta y = \frac{dy}{dx} \cdot \Delta x$	$(x + \Delta x, y + \Delta y)$
(0, 1)				

$$\frac{dy}{dx} = e^{xy} \quad (0,1) \quad \Delta x = .2$$

$(x, y)$	$\frac{dy}{dx}$	$\Delta x$	$\Delta y$	$(x, y)$
(0, 1)	1	.2	.2	(-.2, -.8)
(-.2, -.8)	.85214	.2	-.17043	(-.4, .62957)
(-.4, .62957)	.77738	.2	-.15578	(-.6, .47409)
(-.6, .47409)	.75242	.2	-.15048	(-.8, .32361)
(-.8, .32361)	.72191	.2	-.14438	(-1, .16923)

$$f(-1) \approx .169$$



## Homework

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